

# CHEM 133 FINAL EXAM

May 19, 2016

## SOLUTIONS

Equations and constants that you may find useful:

Equation for voltage across resistor in RC circuit as a function of time for a step change of  $\Delta V_{in}$  at time  $t = 0$ :

$$V_R = \Delta V_{in} e^{-t/RC}$$

Standard deviation:

$$S = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

Digitization equation for n bit digitizer: decimal # =  $(V_{meas} - V_{min}) \cdot 2^n / V_{range}$

Noise Equations: 1) Thermal noise:  $V_{noise}(rms) = (4kTRB)^{1/2}$

2) Shot Noise:  $I_{noise}(rms) = (2eIB)^{1/2}$

k = Boltzmann's constant =  $1.38 \times 10^{-23} \text{ V}^2 \text{ s } \Omega^{-1} \text{ K}^{-1}$ , T = temperature (K), R = resistance, B = bandwidth, I = current, and e = elementary charge =  $1.60 \times 10^{-19} \text{ C}$ . C = coulombs

F = Faraday's constant = 96,500 C/mol e

Units: 1 A = 1 C/s; 1 J = 1 C·V; 1 W = 1 V·A, A = amps, V = volts, W = watts, J = joules

Nernst Equation:

$$E = E^\circ - \frac{RT}{nF} \ln Q = E^\circ - \frac{2.303RT}{nF} \log Q = E^\circ - \frac{0.05916}{n} \log Q \text{ (T = 298 K)}$$

R = Universal Gas Constant =  $8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ ; F = Faraday's constant = 96,500 C/mol e<sup>-</sup>; n = moles e<sup>-</sup>

h = Planck's constant =  $6.626 \times 10^{-34} \text{ J}\cdot\text{s}$ , speed of light in a vacuum = c =  $2.998 \times 10^8 \text{ m/s}$

Dispersion of a grating monochromator:

constructive interference occurs for:  $n\lambda = d(\sin\theta - \cos\phi)$

angular dispersion:  $\frac{\Delta\phi}{\Delta\lambda} = \frac{n}{d\cos\phi}$  linear dispersion:  $\frac{\Delta y}{\Delta\lambda} = \frac{F\Delta\phi}{\Delta\lambda}$

where n = order,  $\theta$  = entrance angle from normal  $\phi$  = exit angle from normal, F = focal length, and d = groove spacing

Boltzmann Distribution:  $N^*/N_0 = (g^*/g_0)e^{-E/kT}$  with Boltzman Constant = k =  $1.38 \times 10^{-23} \text{ J/K}$

0°C = 273 K; Planck's constant h =  $6.626 \times 10^{-34} \text{ J}\cdot\text{s}$

Boltzmann Distribution:  $N^*/N_0 = (g^*/g_0)e^{-E/kT}$  with Boltzman Constant = k =  $1.38 \times 10^{-23} \text{ J/K}$

NMR frequency equation:  $\nu = (\gamma/\pi)B_0$  ( $\nu$  = frequency and  $B_0$  = magnetic field at the nucleus)

Pascal's triangle:

$$\begin{array}{ccccccc}
 & & & & 1 & & & & \\
 & & & & & 1 & & 1 & \\
 & & & 1 & & 2 & & 1 & \\
 & & 1 & & 3 & & 3 & & 1 \\
 1 & & 4 & & 6 & & 4 & & 1
 \end{array}$$

Chromatography Equations: retention factor =  $k = (t_r - t_m)/t_m$

$\alpha = k_y/k_x$  for components x and y (eluting in that order)

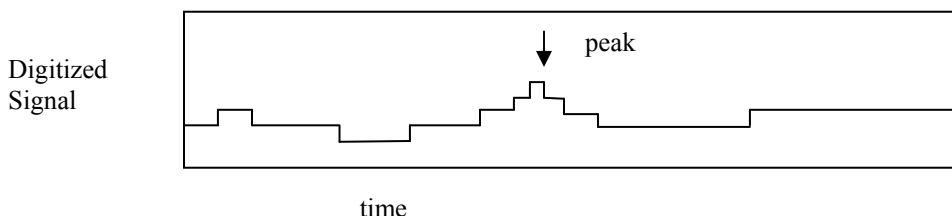
$N = \text{plate number} = 16(t_r/w)^2$  ( $w = \text{width at base}$ )

Resolution optimization equation:  $k_2 = \text{retention factor of second eluting compound}$

$$R_s = \frac{1}{4} \sqrt{N} \left( \frac{\alpha - 1}{\alpha} \right) \left( \frac{k_2}{1 + k_2} \right)$$

SHORT ANSWER SECTION: (Each question worth 3 points)

1. Which electrical device is used to store charge?  
a) diode    **b) capacitor**    c) resistor    d) operational amplifier
2. Which of the following **analog** electronics parts is most commonly used for signal processing?  
a) transducer    b) Excel based moving average  
c) analog to digital convertor    **d) RC filter**
3. A portion of a signal is collected from a GC detector and digitized (through an analog to digital converter). A peak comes out where marked. What is a clear problem with the digitization?



- a) sampling at too high of a frequency    b) input voltage exceeding input range  
**c) not enough bits in digitizer**    d) it is missing the Minecraft people
4. Besides absorption of light, list one other way in which a molecule in the ground state can be excited. Other way = 1) charge particle bombardment, 2) thermally, 3) transition from even higher state (e.g. deactivation from excited electronic + vibrational state), 4) chemical reaction
5. Which of the following monochromator components causes dispersion of light?  
a) collimating optics    **b) grating**    c) focusing optics    d) exit slit
6. The most common atomization method used with atomic emission spectrometers is:  
**a) inductively coupled plasma**    b) electrospray  
c) flame    d) graphite furnace
7. In NMR in order to increase sensitivity, we want to decrease:  
a) the % of active nuclei    **b) the ratio of excited to ground state nuclei**  
c) the number of scans    d) the magnetic field

8. List (give name or describe how it works) a type of mass analyzer in a mass spectrometer.  
Mass analyzer = 1) quadrupole, 2) ion trap, 3) magnetic sector, 4) time of flight, etc.

9. In a liquid – liquid extraction performed using hexane and water buffered to a pH of 6.0, which of the following components is expected to have the highest concentration in the hexane phase.

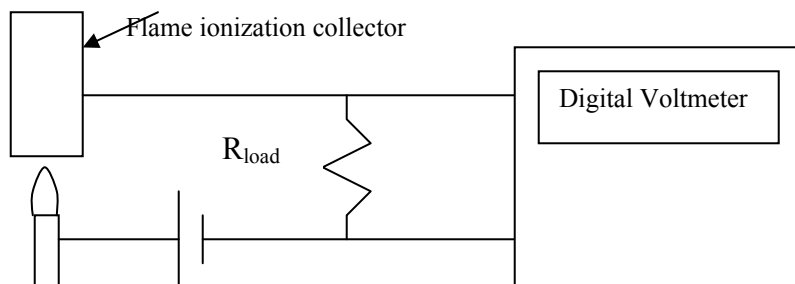
- a)  $C_6H_5OH$  (phenol,  $pK_a$  of  $-OH = 10.00$ ) (only one uncharged at given pH)
- b)  $C_6H_5CO_2H$  (benzoic acid,  $pK_a$  of  $-CO_2H = 4.20$ )
- c)  $C_6H_5CH_2NH_2$  (benzylamine,  $pK_a$  of  $-NH_3^+$  conjugate acid = 9.35)
- d)  $HOC_6H_4CO_2H$  (salicylic acid,  $pK_{a1}$  of  $-CO_2H = 2.97$  and  $pK_{a1}$  of  $-OH = 13.7$ )

10. In capillary GC, which band broadening term is minimal

- a) A (multiple pathways term)
- b) B (longitudinal diffusion term)
- c) C (mass transport term)
- d) u (the flow velocity)

SECTION II. PROBLEM SECTION. Show work – use the back side if needed

1. The following circuit is used to measure the current from a flame ionization detector (FID). The flame ionization collector collects positively charged ions. The load resistor is 6,810 k $\Omega$ . (15 pts)



a) The digital voltmeter (DVM) reads 0.0571 V when a methane flux of  $1.00 \times 10^{-9}$  mol/s goes to the detector, what current is being produced by the FID? Assume no current goes to the digital voltmeter.

$$I = V/R = 0.0571 \text{ V} / 6.81 \times 10^6 \Omega = 8.38 \times 10^{-9} \text{ A} (= 8.38 \text{ nA})$$

b) If the DVM has non-infinite internal resistance, will the true current be greater or less than the measured current? Explain your answer.

$$I_{FID} = I_R + I_{DVM} \text{ (Kirchhoff's current law)} = I_{true} \text{ while } I_{meas} = I_R$$

so  $I_{true} > I_{meas}$

c) If the noise level (the standard deviation in the voltage readings when no hydrocarbon goes to the detector) is 0.0008 V, what is the minimum detectable flux of methane (the flux level capable of giving a signal of 3x the noise)?

Assume there is no DVM error and the FID response is linear with methane flux.

$$LOD \text{ signal} = 3noise = 3(0.0008 \text{ V}) = 0.0024 \text{ V. } (V_{LOE}/V_{sample}) = (F_{LOD}/F_{sample}) \text{ (} F = \text{flux)}$$

$$F_{LOD} = (0.0024 \text{ V} / 0.0571 \text{ V})(1.00 \times 10^{-9} \text{ mol/s}) = 4.2 \times 10^{-11} \text{ mol/s}$$

2. A chemist is testing an electrode for measuring  $\text{Cd}^{2+}$  in solution by using the following cell:  $\text{Cd(s)}|\text{Cd}^{2+}(\text{aq}, 1.0 \text{ M})||\text{KCl}(\text{aq}, 1.0 \text{ M})|\text{AgCl(s)}|\text{Ag(s)}$ . Given the  $E^\circ$  for the following reactions, calculate the cell potential (remember in the cell notation that the left half is for oxidation). (8 pts)

Standard reduction potentials:  $\text{Cd}^{2+}(\text{aq}) + 2\text{e}^- \leftrightarrow \text{Cd(s)}$   $E^\circ = -0.380 \text{ V}$

$\text{AgCl(s)} + \text{e}^- \leftrightarrow \text{Ag(s)} + \text{Cl}^-(\text{aq})$   $E^\circ = 0.222 \text{ V}$

*left half = anode = oxidation, right half = reduction*

$E_{\text{cell}} = E_{\text{cathode}} - E_{\text{anode}}$  *note: all conditions are standard so we can replace  $E_{\text{cathode}}$  with  $E^\circ (= 0.222 \text{ V})$  and  $E_{\text{anode}}$  with  $E^\circ (= -0.380 \text{ V})$  or*

$E_{\text{cell}} = 0.222 \text{ V} - (-0.380 \text{ V}) = \mathbf{0.602 \text{ V}}$

3. Atomic emission spectrometers for inductively coupled plasmas (ICPs) often use polychromators (dispersion of light to an array of detection elements) instead of standard grating monochromators. (12 pts)

a) What component of a monochromator is not present with a polychromator?

**Exit slits.** *These are replaced with the detector elements. Also, **grating rotation** is not required as all wavelengths are emitted at fixed angles to the different detector elements.*

b) What is the advantage to using a polychromator (as opposed to a scanning monochromators) for atomic emission spectroscopy?

*It allows simultaneous analysis of multiple elements since several detectors can be record emissions data at once (no need to rotate grating). This allows faster analysis as there is no need for rotation of the grating to go from one element to another.*

c) These polychromators typically are designed for high resolution measurements. Why is this desirable for atomic emission spectrometry?

*Because emission bands for atomic spectroscopy are very narrow. Having high resolution means a better signal.*

4. 1,2-dichloropropane ( $\text{CH}_3\text{CH}(\text{Cl})\text{CH}_2\text{Cl}$ ) is analyzed by  $^1\text{H}$  NMR. It is observed to have a jumbled multiplet (unclear number of split peaks) at 4.1 ppm, and simpler peaks at 3.6 and 1.6 ppm. (10 pts)

a) Indicate which protons are giving the signals at each peak.

*4.1 ppm is middle H ( $\text{CHCl H}$ ). This is known because it is split by two other sets of Hs and because it is the most electronegative.*

*3.6 ppm is the right  $\text{CH}_2$  protons (second most electronegative).*

*1.6 ppm is the  $\text{CH}_3$  group protons (least electronegative)*

b) Predict the splitting pattern (e.g. triplet) observed at 3.6 and 1.6 ppm.

*Both are **doublets** split by the central CH proton.*

5. Upon analysis by mass spectrometry 1,1-bromo-chloro-ethane ( $\text{CHBrClCH}_3$ ) gives a most common isotope peak of 142. Given information for less common isotopes below, give ratios of peak intensities for  $M+1/M$  (e.g. ratio of intensity of 143 peak to 142 peak),  $M+2/M$  and  $M+4/M$  ratios. The most common isotopes are:  $^{12}\text{C}$ ,  $^{35}\text{Cl}$ , and  $^{79}\text{Br}$

Isotope/Element	C	Cl	Br
M	100	100	100
M+1	1.08	none	none
M+2	none	32	97

You can ignore the contribution of 2  $^{13}\text{C}$ s to any ratios. (9 pts)

$M+1/M$  – all from C. Two Cs means  $2(1.08)/100 = \mathbf{2.16/100}$  (or 0.0216)

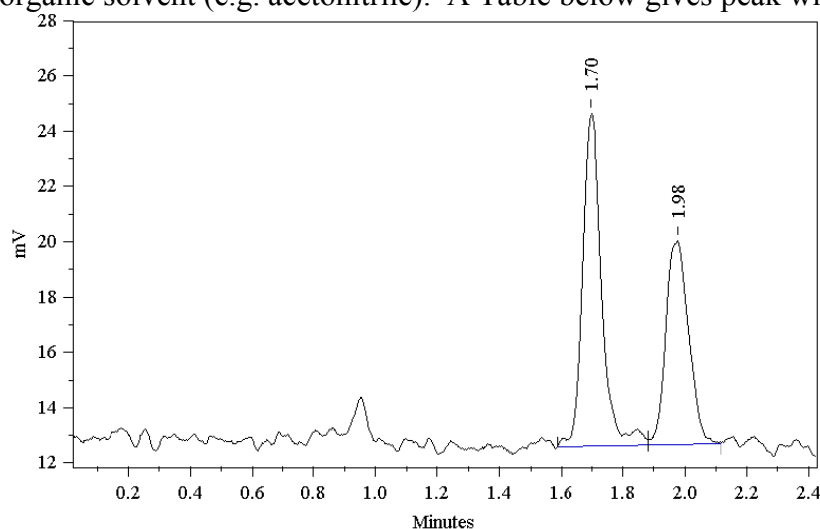
$M+2/M$  – from Cl and Br (either 1  $^{37}\text{Cl}$  or 1  $^{81}\text{Br}$  – since or we add numbers)

$M+2/M = 32/100 + 97/100 = \mathbf{129/100} = 1.29$

$M+4/M$  – requires both a 1  $^{37}\text{Cl}$  and 1  $^{81}\text{Br}$  (must multiply numbers)

$M+4/M = [(32)(97)/100]/100 = \mathbf{31/100} = 0.31$

6. The chromatogram below shows the separation of glucose (1.70 min) from levoglucosan (1-6-anhydro- $\beta$ -glucose) (1.98 min). The chromatogram was obtained with a 150 mm length C18 column using 90% water, 10% acetonitrile at a flow rate of 1.0 mL/min. Note: that water is the most polar solvent for this column, and it is not possible to use the column with less than 10% organic solvent (e.g. acetonitrile). A Table below gives peak widths and areas. (16 pts)



Name	Ret. Time (min)	Conc. (mg/L)	Peak Height (mV)	Width at base (min)
Unretained	0.95	-	-	-
glucose	1.70	1.0	12.05	0.115
levoglucosan	1.98	1.0	7.36	0.133

a) Choosing one peak, calculate the plate number (N) and plate height (H, in mm) of the column.

glucose:  $N = 16(1.70/0.115)^2 = \mathbf{3500}$  levoglucosan:  $N = 16(1.98/0.133)^2 = \mathbf{3550}$

b) Determine retention factor (k) of glucose and the resolution ( $R_s$ ) between glucose and levoglucosan.

$$k = (1.70 - 0.95)/0.95 = \mathbf{0.79}$$

$$\text{resolution} = \Delta t_r/w_{ave} = (1.98 - 1.70)/[0.5(0.115 + 0.133)] = \mathbf{2.26}$$

c) If a chemist was planning on using this column to analyze samples that had five to ten sugars present (in addition to glucose and levoglucosan) under current conditions, is it likely that all the sugars would be well resolved? Assume the other sugars have similar polarity. Explain your answer.

**NO.** *The values for k are small, meaning it would be likely that there would be overlapping sugar peaks.*

Bonus) For the situation in c), could any changes be made to improve the analysis? would it require a different column or just different solvents? (3 pts)

*Unfortunately, a new column would be required because, to improve separation, we would want to increase retention. However, this would require a more polar solvent, which is not possible.*  
(+ 2 pts)

*It is likely with a column that is more retentive to sugars, a successful separation would occur.*  
(+1 pt)