## CHEMISTRY 31

Quiz 2-10 minutes
Sept. 21
KEY

1. A student prepares an $\mathrm{Al}^{3+}$ solution by dissolving an Al foil square into hydrochloric acid. After dissolution, the solution is transferred to a $50.0 \pm 0.1 \mathrm{~mL}$ volumetric flask and diluted to the line. The square is measured to have a length of $1.00 \pm 0.04 \mathrm{~cm}$ and a thickness of $0.173 \pm 0.008$ mm . Given that Al has a density of $2.699 \mathrm{~g} \mathrm{~cm}^{-3}$, determine the concentration in $\mathrm{g} / \mathrm{L}$ and the absolute uncertainty in $\mathrm{g} / \mathrm{L}$ of the solution. Give the final answers with the correct number of significant figures.


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\mathrm{Vol}=e^{2} t
$$

Conc. $=$ mass $A l /\left(\right.$ vol sol' $n$ ) where mass $A l=($ vol metal $)($ density $)=l^{2} t \cdot d e n s i t y /(v o l ~ s o l ' n)$
Conc. $=(1.00 \mathrm{~cm})^{2}(0.173 \mathrm{~mm})(1 \mathrm{~cm} / 10 \mathrm{~mm})\left(2.699 \mathrm{~g} \mathrm{~cm}^{-3}\right)(1000 \mathrm{~mL} / \mathrm{L}) /(50.0 \mathrm{~mL})$
Conc. $=0.9339 \mathrm{~g} / \mathrm{L}$
For propagation of uncertainty, this is a mixed operation problem with exponent $\left(l^{2}\right)$ and multiplication division in it (the rest)
$\left.\operatorname{Unc}\left(l^{2}\right) /\left(l^{2}\right)=2(\operatorname{Unc}(l)) / l\right)=2(0.04 / 1.00)=0.08$ (note: this is a relative unc and can be transferred directly as such to the second equation)
$\operatorname{Unc}($ Conc $) /$ Conc $=\left\{\left[\operatorname{Unc}\left(l^{2}\right) /\left(l^{2}\right)\right]^{2}+[U n c(t) / t]^{2}+[U n c(v o l) / V o l]^{2}\right\}^{0.5}$
$=\left[(0.08)^{2}+(0.008 / 0.173)^{2}+(0.1 / 50.0)^{2}\right]^{0.5}=0.092$
Absolute unc. In conc. $=(0.092)(0.9339 \mathrm{~g} / \mathrm{L})=0.086$
Conc. $\pm$ unc $=0.93 \pm 0.09 \mathrm{~g} / \mathrm{L}$

