# Chapter 10: Determining How Costs Behave 

## Horngren 13e

## The Linear Cost Function



## ANALYSIS OF MIXED COSTS: HIGH-LOW METHOD

EXAMPLE: Kohison Company has incurred the following shipping costs over the past eight months:

|  | Units <br> Sold | Shipping <br> Cost |
| :--- | ---: | ---: |
| January... | $\mathbf{6 , 0 0 0}$ | $\$ 66,000$ |
| February. | $\mathbf{5 , 0 0 0}$ | $\$ 65,000$ |
| March ..... | $\mathbf{7 , 0 0 0}$ | $\$ 70,000$ |
| April....... | $\mathbf{9 , 0 0 0}$ | $\$ 80,000$ |
| May....... | $\mathbf{8 , 0 0 0}$ | $\$ 76,000$ |
| June....... | $\mathbf{1 0 , 0 0 0}$ | $\$ 85,000$ |
| July....... | $\mathbf{1 2 , 0 0 0}$ | $\$ 100,000$ |
| August... | $\mathbf{1 1 , 0 0 0}$ | $\$ 87,000$ |

With the high-low method, only the periods in which the lowest activity and the highest activity occurred are used to estimate the variable and fixed components of the mixed cost.

## EVALUATION OF THE HIGH-LOW METHOD



## Regression Analysis

- Regression analysis is a statistical method that measures the average amount of change in the dependent variable associated with a unit change in one or more independent variables
- Is more accurate than the High-Low method because the regression equation estimates costs using information from all observations; the High-Low method uses only two observations


## LEAST-SQUARES REGRESSION METHOD

The least-squares regression method for analyzing mixed costs uses mathematical formulas to determine the regression line that minimizes the sum of the squared "errors."


## Sample Regression Model Plot



Learning Objective 1: Explain the two assumptions frequently used in cost-behavior estimation . . . cost functions are linear and have a single cost driver

Write a linear cost function equation for each of the following conditions. Use y for estimated costs and X for activity of the cost driver.
a. Direct manufacturing labor is $\$ 10$ per hour.
b. Direct materials cost $\$ 9.20$ per cubic yard.
c. Utilities have a minimum charge of $\$ 1,000$, plus a charge of $\$ 0.05$ per kilowatt-hour.
d. Machine operating costs include \$200,000 of machine depreciation per year, plus $\$ 75$ of utility costs for each day the machinery is in operation.

## Learning Objective 4: Estimate a cost function using quantitative analysis . . . the end result is to evaluate the cost driver of the estimated cost function

The managers of the production department have decided to use the production levels of 20X2 and 20X4 as examples of the highest and lowest years of operating levels. Data for those years are as follows:

| $\frac{\text { Year }}{20 X 2}$ | $\frac{\text { Chemicals used }}{140,000 \text { gallons }}$ |  | Overhead Costs <br> 115,000 <br> $20 \times 4$ |
| :--- | :--- | :--- | :--- |
|  | 120,000 gallons |  | $\$ 100,000$ |

## Required:

What is the cost estimating equation for the department if gallons of chemicals are used as the cost driver?

## Learning Objective 4: Estimate a cost function using quantitative analysis . . . the end result is to evaluate the cost driver of the estimated cost function

The Wildcat Company has provided the following information:

| $\underline{\text { Units of Output }}$ | $\underline{30,000}$ Units |  | $\underline{\mathbf{4 2 , 0 0 0} \text { Units }}$ |
| :--- | :---: | :---: | :---: |
| Direct materials | $\$ 180,000$ | $\$ 252,000$ |  |
| Workers' wages | $1,080,000$ | $1,512,000$ |  |
| Supervisors' salaries | 312,000 | 312,000 |  |
| Equipment depreciation | 151,200 | 151,200 |  |
| Maintenance | 81,600 | 110,400 |  |
| Utilities | $\underline{\underline{384,000}}$ | $\underline{\underline{52,188,800}}$ | $\underline{\underline{\$ 2,865,600}}$ |
| Total |  |  |  |

Using the high-low method and the information provided above,
a. identify the linear cost function equation and
b. estimate the total cost at 36,000 units of output.

## Learning Objective 4: Estimate a cost function using quantitative analysis . . . the end result is to evaluate the cost driver of the estimated cost function

Tessmer Manufacturing Company produces inventory in a highly automated assembly plant in Olathe, Kansas. The automated system is in its first year of operation and management is still unsure of the best way to estimate the overhead costs of operations for budgetary purposes. For the first six months of operations, the following data were collected:

|  | Machine-hours | Kilowatt-hours | Total Overhead Costs |
| :---: | :---: | :---: | :---: |
| January | 3,800 | 4,520,000 | \$138,000 |
| February | 3,650 | 4,340,000 | 136,800 |
| March | 3,900 | 4,500,000 | 139,200 |
| April | 3,300 | 4,290,000 | 136,800 |
| May | 3,250 | 4,200,000 | 126,000 |
| June | 3,100 | 4,120,000 | 120,000 |

## Required:

a. Use the high-low method to determine the estimating cost function with machine-hours as the cost driver.
b. Use the high-low method to determine the estimating cost function with kilowatt-hours as the cost driver.
c. For July, the company ran the machines for 3,000 hours and used $4,000,000$ kilowatt-hours of power. The overhead costs totaled $\$ 114,000$. Which cost driver was the best predictor for July?

The new cost analyst in your accounting department has just received a computergenerated report that contains the results of a simple regression program for cost estimation. The summary results of the report appear as follows:

| $\underline{\text { Variable }}$ | $\underline{\text { Coefficient }}$ |  | Standard Error |  |
| :--- | :--- | :--- | :--- | :--- |
| Constant | $\$ 35.92$ | $\$ 16.02$ |  | t-Value |
| Independent variable | $\$ 563.80$ |  | $\$ 205.40$ |  |

$\mathrm{R}^{2}=0.75$
Required:
a. What is the cost estimation equation according to the report?
b. What is the goodness of fit? What does it tell about the estimating equation?
Newton Company used least squares regression analysis to obtain the following output: Payroll Dept Cost
Explained by \# of Employees
Constant ..... \$5,800
Standard error of Y estimate ..... 630
$\mathrm{R}^{2}$ ..... 0.8924
Number of observations ..... 20
X coefficient(s) ..... \$1.902
Standard error of coefficient(s) ..... 0.0966
Required:
a. What is the total fixed cost?
b. What is the variable cost per employee?
c. Prepare the linear cost function.
d. What is the coefficient of determination? Comment on the goodness of fit.

Schotte Manufacturing Company uses two different independent variables (machine-hours and number of packages) in two different equations to evaluate costs of the packaging department. The most recent results of the two regressions are as follows:

## Machine-hours:

| Variable | Coefficient |  | Standard Error |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Constant | $\$ 748.30$ |  | $\$ 341.20$ |  |
| Independent Variable | $\$ 52.90$ |  | $\$ 35.20$ |  | 1.50 |

$\mathrm{R}^{2}=0.33$
Number of packages:

| Variable | Coefficient |  | Standard Error |  | -Value |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Constant | $\$ 242.90$ |  | $\$ 75.04$ |  |
| Independent Variable | $\$ 5.60$ |  | $\$ 2.00$ |  |  |

$\mathrm{R}^{2}=0.73$
Required:
a. What are the estimating equations for each cost driver?
b. Which cost driver is best and why?

