

CPE 64 PAL Worksheet ECS, CSUS

r's and (r-1)'s complement worksheet

- 1) For binary number arithmetic, what is the advantage of using 2's complement?
- 2) For binary number arithmetic, what is the disadvantage of using 2's complement?

Example1) Find the 9's complement of $N = 546700$.

Solution: The formula for 9's complement is $(r^n - 1) - N$

(where n is the numbers of digits in the number N, r is the base of the number system. Here $r = 10$, because it is a base 10 number, $n = 6$, because there are 6 digits in the given N.)

$$999999 - 546700 = 453299 \text{ (9's complement)}$$

9's complement of 546700 is 453299

- 3) Find the 9's complement of 27785936.
- 4) Find the 9's complement of 00000000.

Example 2) Find the 10's complement of 72532

$$r^n - N = [(r^n - 1) - N] + 1$$

$$99999 - 72532 = 27467 \text{ (9's complement)}$$

$$27467 + 1 = 27468 \text{ (10's complement)}$$

10's complement of 72532 is 27468

- 5) Find the 10's complement of 576325800.
- 6) Find the 10's complement of 948571236.

Example 3) Using 10's complement, subtract $72532 - 3250$.

$$3,250 \rightarrow 96,749 \text{ (9s comp)} \rightarrow 96,750 \text{ (10s comp)}$$

$$72532 - 3250 = 72532 + 96750 = 169282 \text{ (Negative)}$$

$$169282 - 100000 \text{ (Discard end carry } 10^5) = 69282$$

Result: $72532 - 3250 = 69282$.

- 7) Perform subtraction on the given unsigned numbers $647813 - 519297$ using the 10's complement of the subtrahend.
- 8) Perform subtraction on the given unsigned numbers $197076 - 375217$ using the 10's complement of the subtrahend.

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- 9) Perform subtraction on the given unsigned numbers $878631 - 745873$ using the 10's complement of the subtrahend.

Example 4) Find the 1's complement of 010010

$$111111 - 010010 = 101101$$

1's complement of 010010 is 101101

- 10) What is the 1's complement of 1001_0110?

- 11) What is the 1's complement of 1101_1011

Example 4) Find the 2's complement of 1010_0101

$$1111_1111 - 1010_0101 = 0101_1010 \text{ (1's complement)}$$

$$0101_1010 + 0000_0001 = 0101_1011 \text{ (2's complement)}$$

2's complement of 1010_0101 is 0101_1011

- 12) Two's complement of the binary number 1010_0101.

- 13) Two's complement representation of value 1101_1110 is.

- 14) What is the largest positive value that can be represented by an 8 bit 2's complement number?

- 15) The range of numbers represented by an 8-bit two's complement representation is.

- 16) Perform subtraction on the unsigned binary numbers $10011 - 10010$ using the 2's complement of the subtrahend.

- 17) Perform subtraction on the unsigned binary numbers $1001 - 110101$ using the 2's complement of the subtrahend.