

Math 12 – Workshop #20

1. Write the imaginary number in simplified form

(a) $\sqrt{-16}$

(b) $\sqrt{-10}$

2. Divide and write the expression in standard form. Assume a and b are real numbers which are not both zero.

(a) $\frac{7}{2-i}$

(c) $\frac{2+9i}{2-9i}$

(b) $\frac{1}{3+4i}$

(d) $\frac{1}{a+bi}$

3. Let $\omega = -\frac{1}{2} + \frac{\sqrt{3}}{2}i$. Compute the following

| | | | | | | |
|------------|-----|--------------------------------------|------------|-----|------------|-----|
| ω | $=$ | $-\frac{1}{2} + \frac{\sqrt{3}}{2}i$ | ω^4 | $=$ | ω^7 | $=$ |
| ω^2 | $=$ | | ω^5 | $=$ | ω^8 | $=$ |
| ω^3 | $=$ | | ω^6 | $=$ | ω^9 | $=$ |

Use the pattern to find ω^{33} , ω^{97} and ω^{1246}

4. Use the square root property to solve

(a) $x^2 = 9$

(c) $(x+3)^2 = 4$

(b) $(x-2)^2 = 9$

(d) $(x-1)^2 - 3 = 0$

5. Fill in the blank to make the following equations true

(a) $x^2 + 6x + \underline{\hspace{2cm}} = (x+3)^2$

(b) $x^2 + 3x + \underline{\hspace{2cm}} = \left(x + \frac{3}{2}\right)^2$

6. What number could you add to both sides of the following equations to make the left hand side a perfect square?

(a) $x^2 + 6x = 1$

(b) $x^2 + 3x = 2$

(c) $x^2 + 5x = 1$

7. Complete the square to solve.

(a) $x^2 + 2x = 4$

(c) $\frac{5x-1}{-3} = x^2$

(b) $x^2 + 4x = 5$

(d) $x^2 - 14x + 50 = 0$

8. Suppose that m is a real number. For each of the following solve for x by completing the square

(a) $x^2 + 4x + m = 0$

(b) $x^2 + mx + 1 = 0$