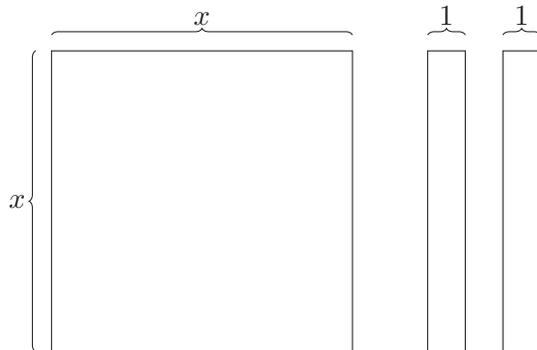


Math 12 – Workshop #22

1. Suppose you are trying to tile a bathroom floor. Consider the three tiles below:



- What is the area of the three tiles shown?
- The three given pieces of tile can *almost* be arranged into a square with sides of length $x + 1$. What is the area of the smallest additional tile you would need in order to make this square?
- Give the area of the three tiles in terms of the area of the larger square.
- Suppose we started with 4 of the above rectangles instead of two. What is the area of the smallest additional tile you would need in order to make a square with sides of length $x + 2$?
- Suppose you were given 6 of the above rectangles instead of two. What is the area of the smallest additional tile you would need in order to make a square with sides of length $x + 3$?
- Suppose you were given b of the above rectangles instead of two. What is the area of the smallest additional tile you would need in order to make a square with sides of length $x + \frac{b}{2}$?

2. Solve the following equations for x by completing the square

(a) $x^2 + 2x + 2 = 0$

(b) $x^2 + x + 1$

(c) $4x^2 - 7x = 1$

- The sum of squares of three consecutive integers, x , $x + 1$ and $x + 2$, is 245, what are the integers?
- The difference between the cubes of two consecutive integers is 271. What are the integers?
- The discriminant of a quadratic polynomial $f(x) = ax^2 + bx + c$ is $b^2 - 4ac$. Look at the quadratic formula and match the statements on the left with the equivalent statements on the right:

(a) $b^2 - 4ac < 0$

i The polynomial f has a single real root

(b) $b^2 - 4ac > 0$

ii The polynomial f has two complex roots

(c) $b^2 - 4ac = 0$

iii The polynomial f has two real roots

6. Determine how many solutions the equations have and if the solutions are complex or real numbers

(a) $5x = x^2 + 3$

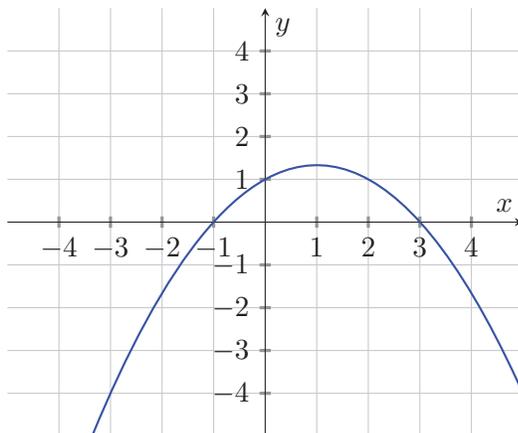
(b) $19x^2 + \frac{5}{2}x + \frac{1}{12} = 0$

(c) $\frac{3}{4}x^2 + 3x + \pi = 0$

7. Given $x^2 + 3x + k$ find all the values of k which give

- (a) Two real solutions. (b) One real solution. (c) Two complex solutions.

8. Below is a graph of a quadratic function of the form $f(x) = ax^2 + bx + c$.



- (a) For which x do we have $f(x) = 0$
(b) Is the discriminant of f positive, negative or zero?
(c) What is $f(0)$?
(d) Which of the following is the equation of f and how do you know?

- i. $f(x) = \frac{1}{2}(x - 1)(x + 3)$ iii. $f(x) = -(x + 1)(x - 3)$
ii. $f(x) = -\frac{1}{3}(x - 1)(x + 3)$ iv. $f(x) = -\frac{1}{3}(x + 1)(x - 3)$

(e) Try to construct the equation for the following quadratic graph.

