Math 29 PAL Worksheet 4

1. If the point (-3,7) is on the graph of an equation, what other point(s) must be on the graph if the graph is symmetric about . . .

- a. the x-axis.
- b. the *y*-axis.
- c. the origin.
- d. both the x- and y-axis.
- 2. The graph of a function f contains the point (2, -5).
 - a. The graph of a function g is obtained by shifting the graph of f 3 units to the right, then 2 units upward, then reflecting in the y-axis. Find a point on the graph of g.
 - b. The graph of a function h is obtained by shifting the graph of f 4 units to the left, then 6 units downward, then reflecting in the x-axis. Find a point on the graph of h.

3. Find the function g that is finally graphed after the following three transformations are applied to the graph of f(x) = |x|.

- Shift left 3 units.
- Shift up 5 units.
- Reflect about the *y*-axis.

4. Consider the graph of $f(x) = x^2$. Explain why compressing the graph of f horizontally toward the *y*-axis by a factor of 3 gives the same result as stretching the graph vertically away from the *x*-axis by a factor of 9.

5. Let $f(x) = 3x^2 + 4x$. In each case, a function g is given whose graph can be obtained from the graph of f by performing a single transformation (that is, a shift left, right, up or down, a reflection in either the x-axis or y-axis, a stretch or compression by some factor away from or toward either the x-axis or y-axis). Describe the transformation that will transform the graph of f into the graph of g.

a. $g(x) = 3x^2 - 4x$ b. $g(x) = 3x^2 + 4x - 2$ c. $g(x) = 6x^2 + 8x$ d. $g(x) = 27x^2 + 12x$ e. $g(x) = \frac{3}{4}x^2 + 2x$ f. $g(x) = -3x^2 - 4x$ g. $g(x) = 3(x - 1)^2 + 4(x - 1)$