Math 29
PAL Worksheet 8

1. If possible, write the function $f(x)=2 x^{2}-x-2$ in the form $f(x)=a\left(x-r_{1}\right)\left(x-r_{2}\right)$ where $a, r_{1}$ and $r_{2}$ are real numbers. If it is not possible to write $f$ in this form, explain how you know.
2. Let $f(x)=-27(x+4)^{5}(x+2)^{2}(x-1)(x-3)^{3}\left(x^{2}+3 x+5\right)$.
a. What is the degree of $f$ ?
b. Is $f(2)$ positive, negative, or zero?
c. Write a power function (in the form $g(x)=a x^{n}$ ) where the graph of $f$ and the graph of $g$ have the same end behavior.
3. The following graph is that of the function $f(x)=x^{4}+3 x^{3}-9 x^{2}-23 x-12$. Using the graph, guess the factorization of $f$. Check your answer by multiplying out your guess.

4. The graph of a polynomial function $y=f(x)$ is shown.


Answer each question.
a. Is the degree of $f$ even or odd?
b. Is the leading coefficient positive or negative?
c. What is the smallest possible degree of $f$ ?
5. The graph of a polynomial function $y=g(x)$ is shown.


Answer each question.
a. Is the degree of $g$ even or odd?
b. Is the leading coefficient positive or negative?
c. What is the smallest possible degree of $g$ ?

