Math 29
PAL Worksheet 9

1. A rectangular box with a square base and no top is to made from 48 square feet of material. If $x$ represents the length of one edge of the square base, write the volume $V$ of the box as a function of $x$.

2. One of the following graphs is the graph of $f(x)=-5(x+3)^{2}(x+1)^{3}(x-2)^{2}(x-3)$. Which is it? Give reasons to support your answer.
I.

III.

II.

IV.

3. In each case, if possible, find a single polynomial function whose graph has all three of the given characteristics. (You may leave your answer in factored form.) If it is not possible to find such a polynomial, state this fact.
a. $\quad$ Crosses the $x$-axis at -4 and 3 .

- Touches, but does not cross, the $x$-axis at -1 and 2 .
- Has degree 8.
b. $\quad$ Crosses the $x$-axis at -4 and 2 .
- Touches, but does not cross, the $x$-axis at -1 .
- Has degree 6.
c. Never touches the $x$-axis.
- Has $y$-intercept -8 .
- Has degree 7 .
d. - Crosses the $x$-axis at $-4,-2$, and 3 , and does not even touch the $x$-axis anywhere else.
- Has degree 7 .
- Whenever $x<-4, f(x)>0$.

