## Math 29 PAL Worksheet 9

1. A rectangular box with a square base and no top is to made from 48 square feet of material. If x represents the length of one edge of the square base, write the volume V of the box as a function of x.



2. One of the following graphs is the graph of  $f(x) = -5(x+3)^2(x+1)^3(x-2)^2(x-3)$ . Which is it? Give reasons to support your answer.

II.





III.







3. In each case, if possible, find a single polynomial function whose graph has all three of the given characteristics. (You may leave your answer in factored form.) If it is not possible to find such a polynomial, state this fact.

- a. Crosses the x-axis at -4 and 3.
  - Touches, but does not cross, the x-axis at -1 and 2.
  - Has degree 8.
- b. Crosses the x-axis at -4 and 2.
  - Touches, but does not cross, the x-axis at -1.
  - Has degree 6.
- c. Never touches the x-axis.
  - Has y-intercept -8.
  - Has degree 7.
- d. Crosses the x-axis at -4, -2, and 3, and does not even touch the x-axis anywhere else.
  - Has degree 7.
  - Whenever x < -4, f(x) > 0.