

1. Consider the region bounded by the graph of $f(x) = \sqrt{1-x}$, the x -axis, and the y -axis. This region is then rotated about the y -axis.

- (a) Find the volume of the resulting solid using the disk/washer method.
- (b) Find the volume of the resulting solid using the shell method.

2. Integrate the following.

(a) $\int \sqrt{x} \ln x \, dx$

(b) $\int \frac{\sin x}{1 + \cos x} \, dx$

(c) $\int \frac{\arctan x}{1 + x^2} \, dx$

(d) $\int_0^1 x^2 e^x \, dx$

(e) $\int_0^4 \frac{1}{(4-x)^{\frac{3}{2}}} \, dx$

3. Determine whether the following series are absolutely convergent, conditionally convergent, or divergent.

(a) $\sum_{n=1}^{\infty} \frac{(-1)^n n 2^n}{3^{n+1}}$

(b) $\sum_{n=1}^{\infty} \frac{(-1)^n (n^2 + 5n^3)}{\sqrt{n + 9n^4 + 4n^2}}$

(c) $\sum_{n=1}^{\infty} \frac{(-1)^n}{\cos n}$