Math 121: College Geometry

California State University, Sacramento · Department of Mathematics & Statistics

A study of the axioms and theorems of Euclidean geometry. A comparison of several geometric axiom systems and their theorems, including those of some non-Euclidean and finite geometries.

CATALOG DESCRIPTION

Study of the axioms and theorems of Euclidean geometry. A comparison of several geometry axiom systems and their theorems, including those of some non-Euclidean and finite geometries. **Graded**: Graded Student. **Units**: 3.0.

Prerequisites

Math 31; Math 32 or Math 35

Assignments

A variety of reading and problem solving assignments will be part of the course.

EXAMINATIONS

There will be regular midterm examinations and a comprehensive final examination for this course.

Course Outline

- I. Preliminaries (3 4 Weeks)
 - A. Sets, logic, relations, mappings
 - B. The real number system
 - C. Axiom systems, models
 - D. Incidence planes
- II. Absolute Geometry (7 Weeks)
 - A. Incidence axiom and ruler postulate
 - B. Betweenness, segments, rays, convex sets, angles, triangles
 - C. Plane separation and Pasch's postulate
 - D. Congruence, SAS postulate, perpendiculars, inequalities
 - E. Circles
 - F. Isometries
 - G. Saccheri quadrilaterals
- III. Euclid's parallel postulate and Non-Euclidean (hyperbolic) Geometry (4 Weeks)
 - A. Equivalent formulations of the parallel postulate
 - B. Biangles, critical angle, absolute lengths
 - C. Cayley-Klein and Poincare models of hyperbolic geometry
 - D. Independence of the parallel axiom