

Chapter 10

- ① The end point of a titration is the point at which the equivalence point is detected. Usually by the observation of a large change in a property of the solution such as a color change, or change in pH.
- The equivalence point is the point at which just enough titrant has been added to use up all of the original analyte.

② $V_a = 0 \text{ mL}$ $[\text{OH}^-] = 0.100 \text{ M}$
 $[\text{H}^+] = 10^{-14} / 0.100 = 1 \times 10^{-13}$ $\text{pH} = 13.0$

$V_a = 1.0 \text{ mL} : 100.0 \text{ mL} \left| \frac{0.100 \text{ mmol}}{1 \text{ mL}} \right| = \frac{10 \text{ mmol OH}^-}{-1 \text{ mmol}} = \frac{9 \text{ mmol}}{101 \text{ mL}} = 0.089 \text{ M OH}^-$
 $1.0 \text{ mL} \left| \frac{1 \text{ mmol}}{1 \text{ mL}} \right| = 1 \text{ mmol H}^+$ $[\text{H}^+] = 1.12 \times 10^{-13}$ $\text{pH} = 12.9$

$V_a = 5.0 \text{ mL} : 5.0 \text{ mL} \left| \frac{1 \text{ mmol}}{1 \text{ mL}} \right| = 5 \text{ mmol}$
 $10 - 5 = \frac{5 \text{ mmol}}{105 \text{ mL}} = 0.048 \text{ M OH}^-$, $[\text{H}^+] = 2.1 \times 10^{-13} \text{ M}$
 $\text{pH} = 12.7$

$V_a = 9.0 \text{ mL} : 9.0 \text{ mL} = 9 \text{ mmol}$
 $10 - 9 = \frac{1 \text{ mmol}}{109 \text{ mL}} = 9.17 \times 10^{-3} \text{ M OH}^-$
 $[\text{H}^+] = 1.09 \times 10^{-12} \text{ M}$ $\text{pH} = 11.96$

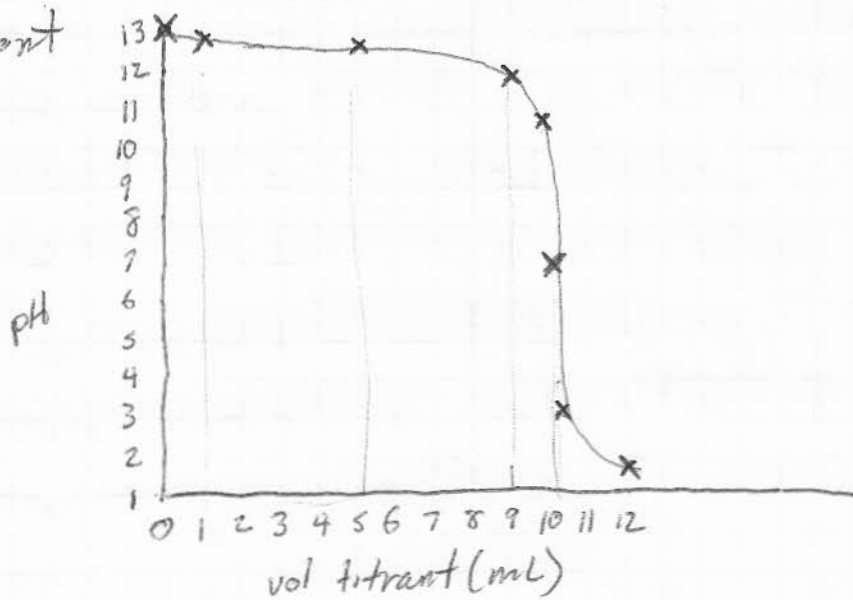
$V_a = 9.9 \text{ mL} : 9.9 \text{ mmol}$
 $10 - 9.9 = \frac{0.1 \text{ mmol}}{109.9} = 9.10 \times 10^{-4} \text{ M OH}^-$
 $[\text{H}^+] = 1.10 \times 10^{-11} \text{ M}$ $\text{pH} = 10.96$

$V_a = 10 \text{ mL} : 10 \text{ mmol}$
 $10 - 10 = 0$ $\text{pH} = 7.00$

$V_a = 10.1 \text{ mL} : 10.1 \text{ mmol} \rightarrow \frac{0.1 \text{ mmol H}^+}{110.1 \text{ mL}} = 9.08 \times 10^{-4} \text{ M H}^+$ $\text{pH} = 3.04$

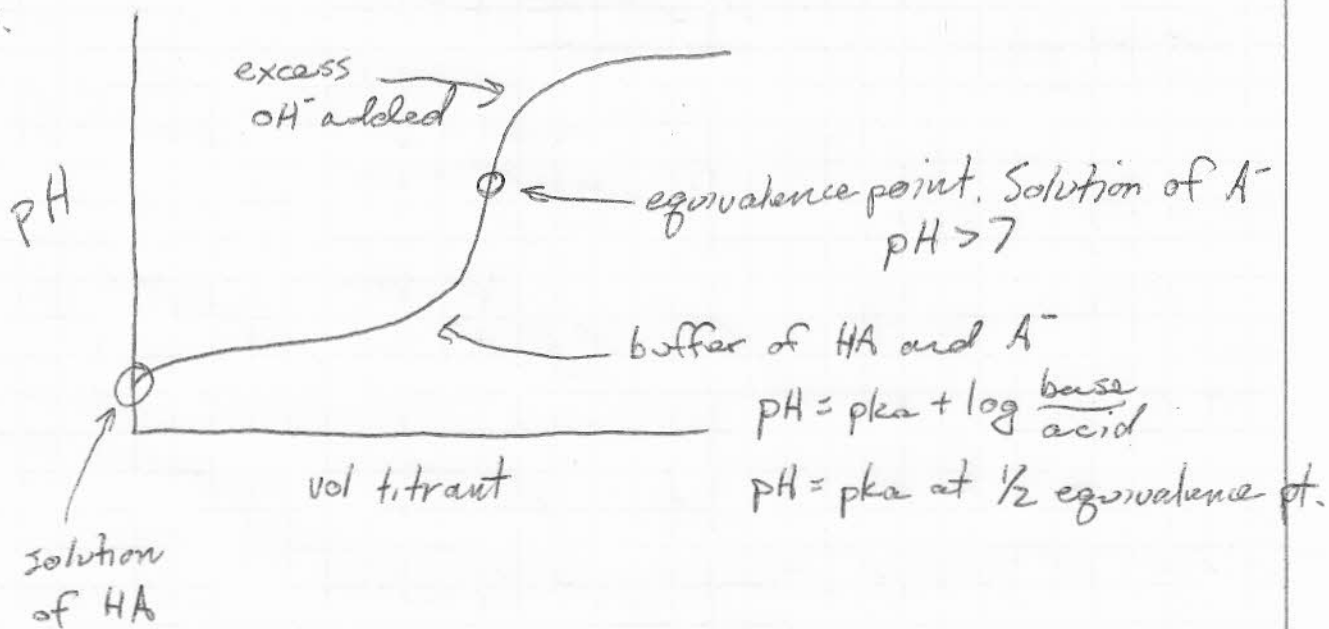
$V_a = 12 \text{ mL} : 12 \text{ mmol} \rightarrow \frac{2 \text{ mmol H}^+}{112 \text{ mL}} = 0.0176 \text{ M H}^+$ $\text{pH} = 1.75$

② cont

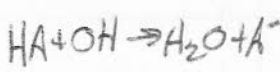


③ The pH scale is logarithmic. ~~Before~~ Before the equivalence point, added titrant is being used up, ~~the pH~~ ~~is not~~ Near the equivalence point the amount of H^+ , or OH^- jumps orders of magnitude, causing the pH to either rise or drop with only a small addition of titrant.

④



⑥ $V_b = 0 \text{ ml}$: $\frac{x^2}{0.100 - x} = 10^{-5}$ $x = 1 \times 10^{-3} = [\text{H}^+]$ $\text{pH} = 3$



$V_b = 1 \text{ ml}$: $100 \text{ mL} \left| \frac{0.100 \text{ mmol}}{1 \text{ mL}} \right| = 10 \text{ mmol} - 1 = 9 \text{ mmol HA}$

$1 \text{ mL} \left| \frac{1 \text{ mmol}}{1 \text{ mL}} \right| = 1 \text{ mmol A}^-$ $\text{pH} = 5.00 + \log \frac{1}{9} = 4.05$

$V_b = 5 \text{ mL}$ $5 \text{ mL} \left| \frac{1 \text{ mmol}}{1 \text{ mL}} \right| = 5 \text{ mmol}$

$10 - 5 = 5 \text{ mmol HA}$ 5 mmol A^- $\text{pH} = 5.00 + \log \frac{5}{5} = 5.00$

$V_b = 9 \text{ mL}$

9 mmol A^- $10 - 9 = 1 \text{ mmol HA}$ $\text{pH} = 5.00 + \log \frac{9}{1} = 5.95$

$V_b = 9.9 \text{ mL}$

9.9 mmol A^- $10 - 9.9 = 0.1 \text{ mmol HA}$ $\text{pH} = 5.00 + \log \frac{9.9}{0.1} = 7.00$

$V_b = 10 \text{ mL}$

- solution of A^- $\frac{10 \text{ mmol}}{110 \text{ mL}} = 0.0909 \text{ M}$ $K_b = 10^{-9}$

$\frac{x^2}{0.0909 - x} = 10^{-9}$

$x = 9.53 \times 10^{-6} \text{ M } [\text{OH}^-]$ $[\text{H}^+] = 1.05 \times 10^{-9}$ $\text{pH} = 8.98$

$V_b = 10.1 \text{ mL}$

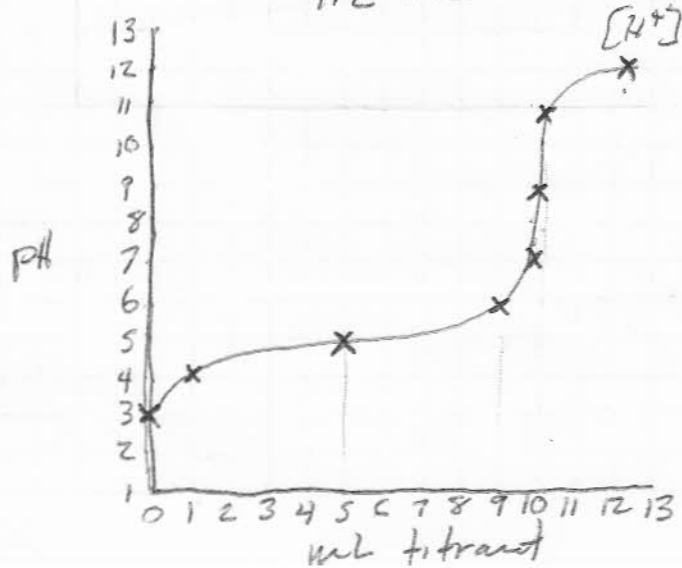
$\rightarrow \frac{0.1 \text{ mmol excess OH}^-}{110.1 \text{ mL}} = 9.08 \times 10^{-4} \text{ M OH}^-$

$[\text{H}^+] = 1.101 \times 10^{-11}$ $\text{pH} = 10.96$

$V_b = 12 \text{ mL}$

$\frac{2 \text{ mmol excess OH}^-}{112 \text{ mL}} = 0.0179 \text{ M OH}^-$

$[\text{H}^+] = 5.6 \times 10^{-13}$ $\text{pH} = 12.25$



8) since the concentration of titrant is $\frac{1}{2}$ concentration of analyte, the volume of titrant needed to reach the equivalence point must be double the original volume of solution. At the equivalence point there is a solution of A^- (hydroxy acetate) with concentration = $\frac{0.100M}{3} = 0.0333M$ $pK_a = 3.832$
 $K_b = 6.79 \times 10^{-11}$

1 part original solution
 2 parts titrant $\rightarrow 3$

$$\frac{x^2}{0.0333-x} = 6.79 \times 10^{-11}$$

$$x = 1.50 \times 10^{-6} = [OH^-] \quad [H^+] = 6.65 \times 10^{-9} \quad \boxed{pH = 8.18}$$

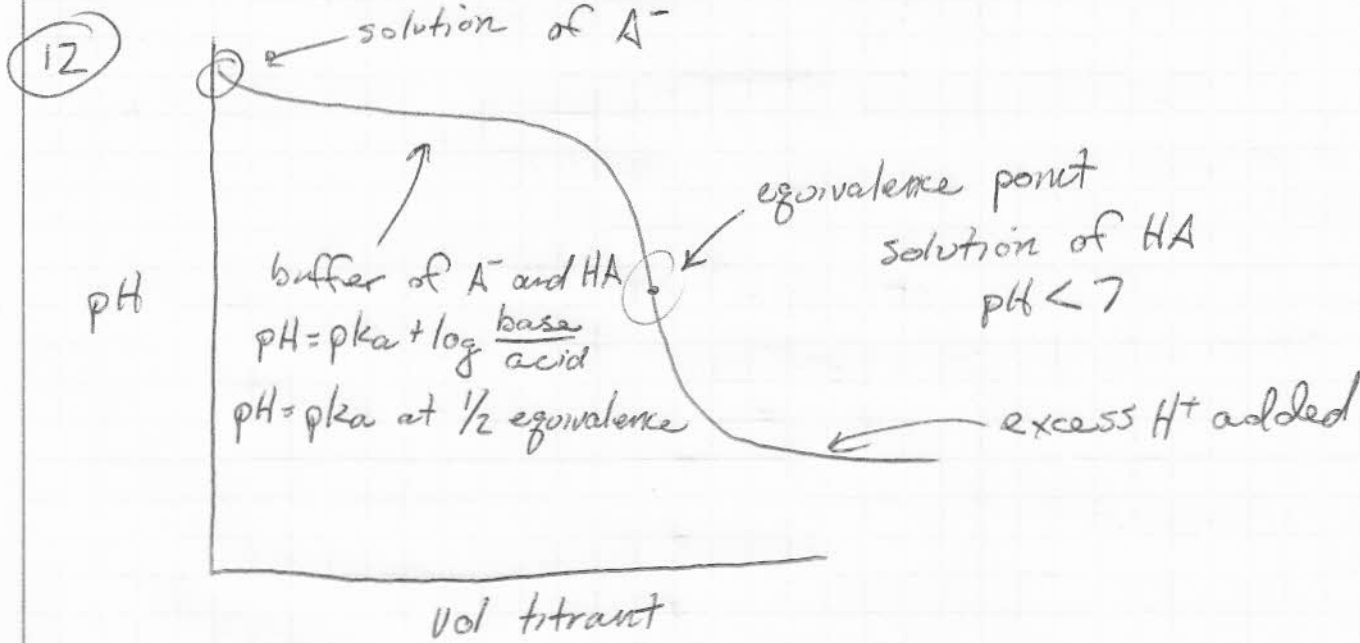
10) $pK_a = 9.39$ $9.24 = 9.39 + \log \frac{\text{base}}{\text{acid}}$ $\frac{\text{base}}{\text{acid}} = 0.708$

base + acid = 5.86×10^{-3} acid = $5.86 \times 10^{-3} - \text{base}$

$$1.214 \text{ g HA} \left| \frac{1 \text{ mol}}{207.29 \text{ g}} \right| = 5.86 \times 10^{-3} \text{ mol HA}$$

$$\frac{\text{base}}{5.86 \times 10^{-3} - \text{base}} = 0.708$$

$$\frac{2.43 \times 10^{-3} \text{ mol OH}^-}{0.02263 \text{ ml}} = \boxed{0.107M} \text{ base} = 2.43 \times 10^{-3} \text{ mol OH}^-$$



(13) At the equivalence point there is a solution of weak acid. The pH must be acidic (< 7).

(14) $V_a = 0 \text{ mL}$: $\frac{x^2}{0.100 - x} = 10^{-5}$
 $x = 1 \times 10^{-3} = [\text{OH}^-] \quad [\text{H}^+] = 10^{-11} \quad \boxed{\text{pH} = 11}$

$V_a = 1.0 \text{ mL}$: $100 \text{ mL} \left| \frac{0.100 \text{ mmol}}{1 \text{ mL}} \right| = 10 \text{ mmol } \text{A}^- \quad \text{A}^- + \text{H}^+ \rightarrow \text{HA}$
 $1.0 \text{ mL} \left| \frac{1.00 \text{ mmol } \text{H}^+}{1 \text{ mL}} \right| = 1 \text{ mmol } \text{A}^-$
 $= 1 \text{ mmol } \text{HA} \quad \text{pH} = 9.00 + \log \frac{9}{1} = \boxed{9.95}$

$V_a = 5.0 \text{ mL}$: $10 - 5 \text{ mmol } \text{A}^- = 5 \text{ mmol } \text{A}^-$
 $5 \text{ mmol } \text{HA} \quad \text{pH} = 9.00 + \log \frac{5}{5} = \boxed{9.00}$

$V_a = 9 \text{ mL}$: $10 - 9 \text{ mmol } \text{A}^- = 1 \text{ mmol } \text{A}^-$
 $9 \text{ mmol } \text{HA} \quad \text{pH} = 9.00 + \log \frac{1}{9} = \boxed{8.05}$

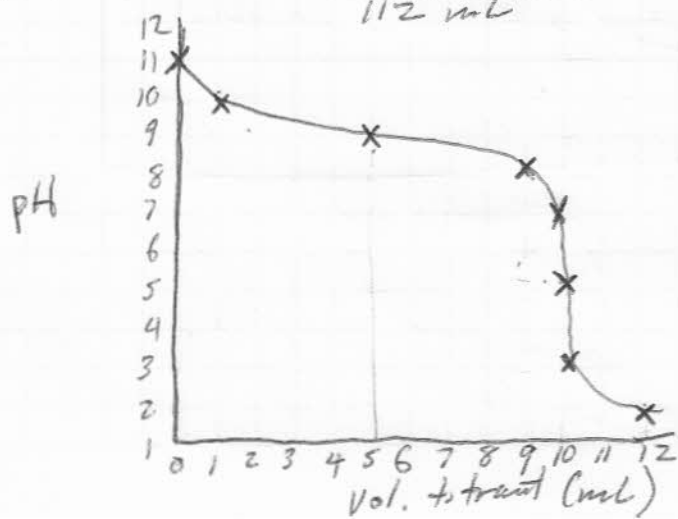
$V_a = 9.9 \text{ mL}$: $10 - 9.9 = 0.1 \text{ mmol } \text{A}^-$
 $9.9 \text{ mmol } \text{HA} \quad \text{pH} = 9.00 + \log \frac{0.1}{9.9} = \boxed{7.00}$

$V_a = 10 \text{ mL}$: $10 - 10 = 0 \rightarrow$ solution of HA $K_a = 10^{-9}$
 $\frac{10 \text{ mmol}}{110 \text{ mL}} = 0.909 \text{ M}$

$\frac{x^2}{0.909 - x} = 10^{-9} \quad x = 9.53 \times 10^{-6} \text{ M} = [\text{H}^+] \quad \text{pH} = \boxed{5.02}$

$V_a = 10.1 \text{ mL}$: $\frac{0.1 \text{ mmol excess } \text{H}^+}{110.1 \text{ mL}} = 9.08 \times 10^{-4} \text{ M } \text{H}^+ \quad \text{pH} = \boxed{3.04}$

$V_a = 12 \text{ mL}$: $\frac{2 \text{ mmol excess } \text{H}^+}{112 \text{ mL}} = 0.0179 \text{ M } \text{H}^+ \quad \text{pH} = \boxed{1.75}$



15) when $HA = A^-$ or half way to the equivalence point

18) $pK_a = 9.21$ $50.0 \text{ mL} \left| \frac{0.100 \text{ mmol}}{1 \text{ mL}} \right| = 5.00 \text{ mmol } A^-$

a. $4.20 \text{ mL} \left| \frac{0.438 \text{ mmol}}{1 \text{ mL}} \right| = 1.84 \text{ mmol } H^+$ $A^- + H^+ \rightarrow HA$

$5.00 - 1.84 = 3.16 \text{ mmol } A^-$
 $1.84 \text{ mmol } HA$ $pH = 9.21 + \log \frac{3.16}{1.84} = \boxed{9.44}$

b. $11.82 \text{ mL} \left| \frac{0.438 \text{ mmol}}{\text{mL}} \right| = 5.18 \text{ mmol } H^+$

$\frac{0.18 \text{ mmol excess } H^+}{61.82 \text{ mL}} = 2.91 \times 10^{-3} \text{ M } H^+$ $pH = \boxed{2.54}$

c. equiv. pt $5.00 \text{ mmol } A^- \left| \frac{1 \text{ mmol } H^+}{1 \text{ mmol } A^-} \right| \left| \frac{1 \text{ mL } H^+}{0.438 \text{ mmol } H^+} \right| = 11.42 \text{ mL } H^+ \text{ added}$

$\frac{5.00 \text{ mmol } HA}{61.42 \text{ mL}} = 0.0814 \text{ M } HA$ $K_a = 6.17 \times 10^{-10}$

$\frac{x^2}{0.0814 - x} = 6.17 \times 10^{-10}$ $x = 7.08 \times 10^{-6} = [H^+]$

$pH = \boxed{5.15}$