



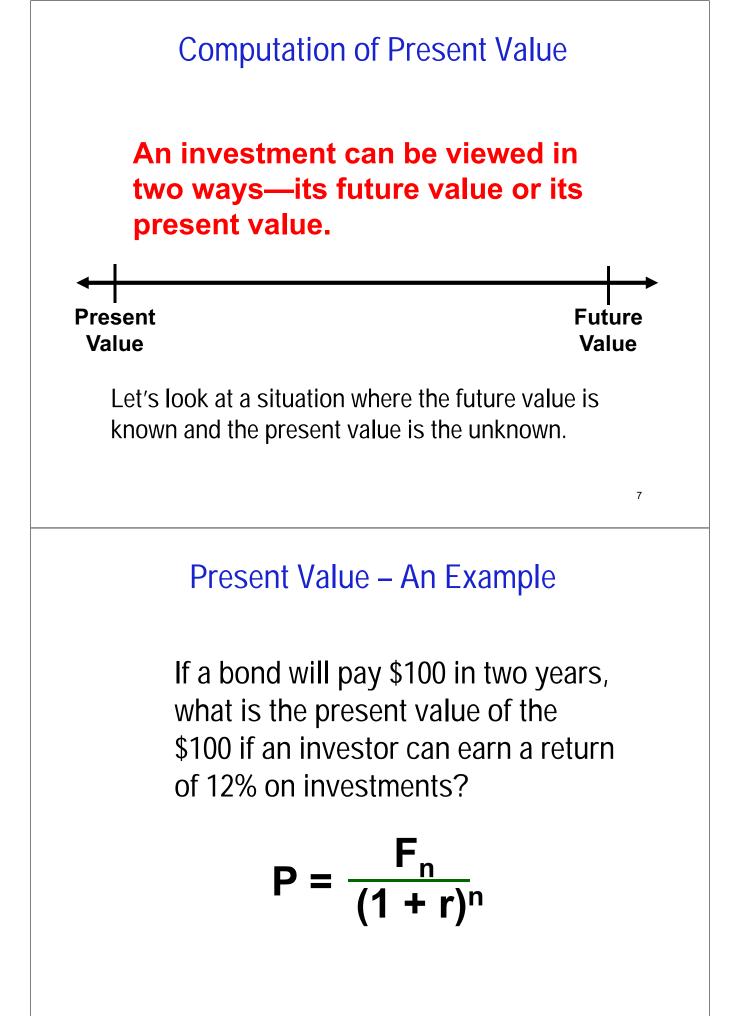
What if the \$108 was left in the bank for a second year? How much would the original \$100 be worth at the end of the second year?

$F_n = P(1 + r)^n$

Compound Interest – An Example

$F_n = \$100(1 + .08)^2$ $F_n = \$116.64$

The interest that is paid in the second year on the interest earned in the first year is known as compound interest.



Present Value – An Example

$P = \frac{\$100}{(1 + .12)^2}$ P = \$79.72

This process is called discounting. We have discounted the \$100 to its present value of \$79.72. The interest rate used to find the present value is called the discount rate.

Present Value – An Example

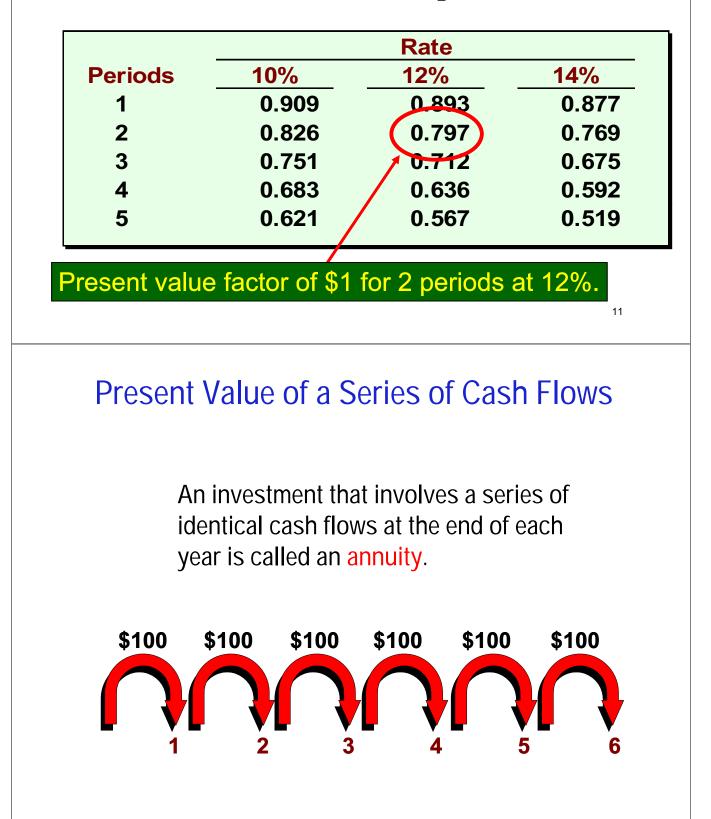
Let's verify that if we put \$79.72 in the bank today at 12% interest that it would grow to \$100 at the end of two years.

	Year 1	Year 2
Beginning balance	\$ 79.72	\$ 89.29
Interest @ 12%	\$ 9.57	\$ 10.71
Ending balance	\$ 89.29	\$100.00

If \$79.72 is put in the bank today and earns 12%, it will be worth \$100 in two years.

Present Value – An Example

\$100 × 0.797 = \$79.70 present value



Present Value of a Series of Cash Flows – An Example

Lacey Inc. purchased a tract of land on which a \$60,000 payment will be due each year for the next five years. What is the present value of this stream of cash payments when the discount rate is 12%?

Present Value of a Series of Cash Flows – An Example

We could solve the problem like this . . .

Present Value of an Annuity of \$1						
Periods	10%	12%	14%			
1	0.909	0.893	0.877			
2	1.736	1.690	1.647			
3	2.487	2.402	2.322			
4	3.170	3.037	2.914			
5	3.791	→ 3.605	3.433			

$60,000 \times 3.605 = 216,300$

General decision rule ...

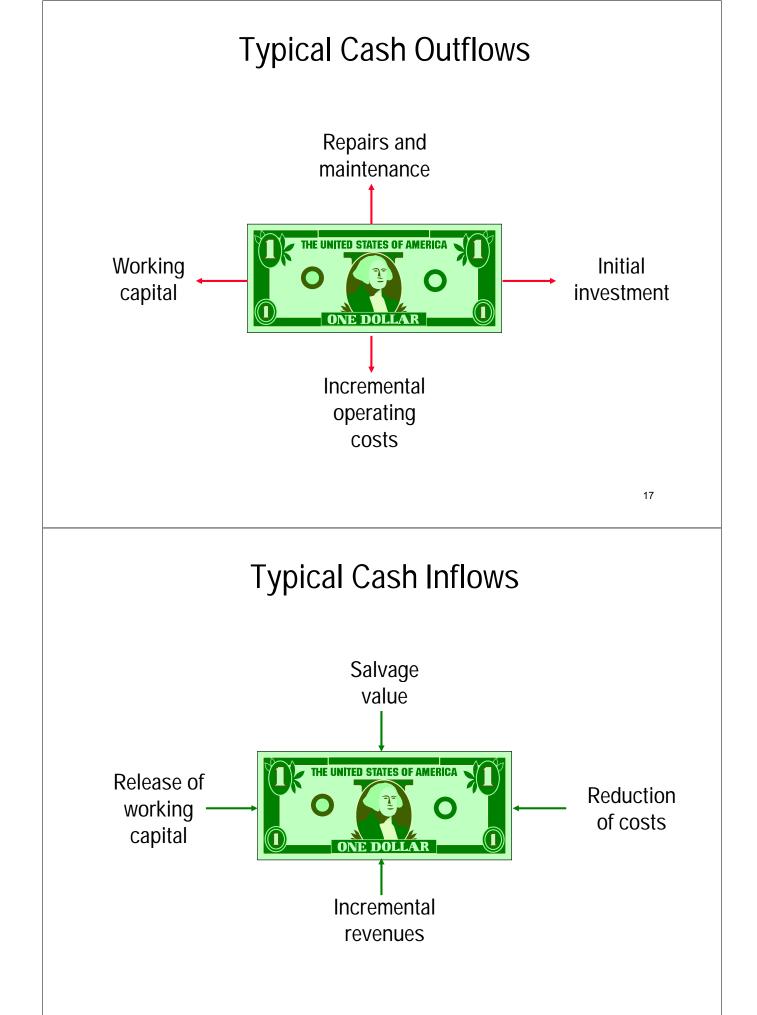
If the Net Present Value is	Then the Project is
Positive	Acceptable, since it promises a return greater than the required rate of return.
Zero	Acceptable, since it promises a return equal to the required rate of return.
Negative	Not acceptable, since it promises a return less than the required rate of return.

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The Net Present Value Method

Net present value analysis emphasizes cash flows and not accounting net income.

The reason is that accounting net income is based on accruals that ignore the timing of cash flows into and out of an organization.



Recovery of the Original Investment

Depreciation is not deducted in computing the present value of a project because . . .

- 1. It is not a current cash outflow.
- 2. Discounted cash flow methods automatically provide for return of the original investment.

Recovery of the Original Investment

Carver Hospital is considering the purchase of an attachment for its X-ray machine.

No investments are to be made unless they have an annual return of at least 10%.

Will we be allowed to invest in the attachment?

Recovery of the Original Investment

			٨٣	nount of	10%	Present Value of Cash
	ltem	Year(s)		sh Flow	Factor	Flows
	llem	Tear(s)	Ua	SITFIOW	Facior	FI0W5
Initial invest	ment (outflow) Now		(3,170)	1.000	(3,170
Annual cash	inflows	1-4	\$	1,000	3.170	\$ 3,170
Net present	value					\$-0-
	Present Va	lue of \$1				
Periods	10%	12%	149	6	(
1	0.909	0.893	0.8	77	Prese	ent value
2	1.736	1.690	1.64	47	of an	annuity
3	2.487	2.402	2.3	22		
4	3.170	3.037	2.9 [°]	14	OT \$	1 table
5	3.791	3.605	3.4	33		/

Recovery of the Original Investment

		(1)		(2)		(3)		(4)		(5)
							Rec	over of	Un	recovered
	Inve	estment					Inve	estment	Inv	estment at
	Outs	standing			Ret	urn on	dur	ing the	the	end of the
	dur	ring the	(Cash	Inve	stment		year		year
Year		year	- h	nflow	(1)	× 10%	(2	2) - (3)		(1) - (4)
1	\$	3,170	\$	1,000	\$	317	\$	683	\$	2,487
2	\$	2,487	\$	1,000	\$	249	\$	751	\$	1,736
3	\$	1,736	\$	1,000	\$	173	\$	827	\$	909
4	\$	909	\$	1,000	\$	91	\$	909	\$	-
Total inv	estme	ent recov	vere	ed		-	\$	3,170	-	

This implies that the cash inflows are sufficient to recover the \$3,170 initial investment (therefore depreciation is unnecessary) and to provide exactly a 10% return on the investment.

Two Simplifying Assumptions

Two simplifying assumptions are usually made in net present value analysis:

All cash flows other than the initial investment occur at the end of periods. All cash flows generated by an investment project are immediately reinvested at a rate of return equal to the discount rate.

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Choosing a Discount Rate

- The firm's cost of capital is usually regarded as the minimum required rate of return.
- The cost of capital is the average rate of return the company must pay to its long-term creditors and stockholders for the use of their funds.

Lester Company has been offered a five year contract to provide component parts for a large manufacturer.

Cost and revenue information				
Cost of special equipment	\$160,000			
Working capital required	100,000			
Relining equipment in 3 years	30,000			
Salvage value of equipment in 5 years 5,000				
Annual cash revenue and costs:				
Sales revenue from parts	750,000			
Cost of parts sold	400,000			
Salaries, shipping, etc.	270,000			

The Net Present Value Method

- At the end of five years the working capital will be released and may be used elsewhere by Lester.
- Lester Company uses a discount rate of 10%.

Should the contract be accepted?

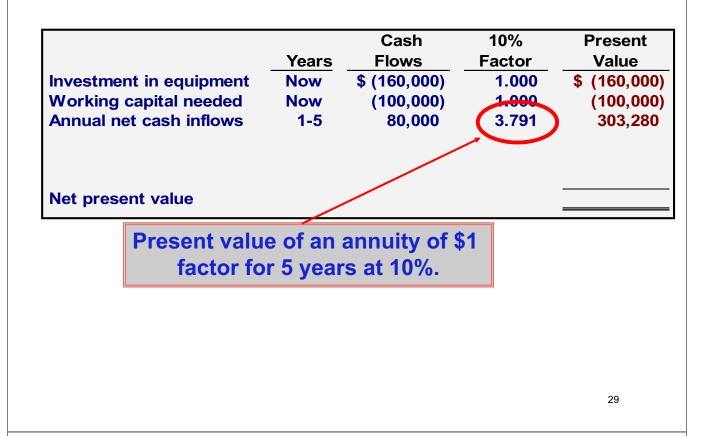
Annual net cash inflow from operations

Sales revenue	\$ 750,000
Cost of parts sold	(400,000)
Salaries, shipping, etc.	(270,000)
Annual net cash inflows	\$ 80,000

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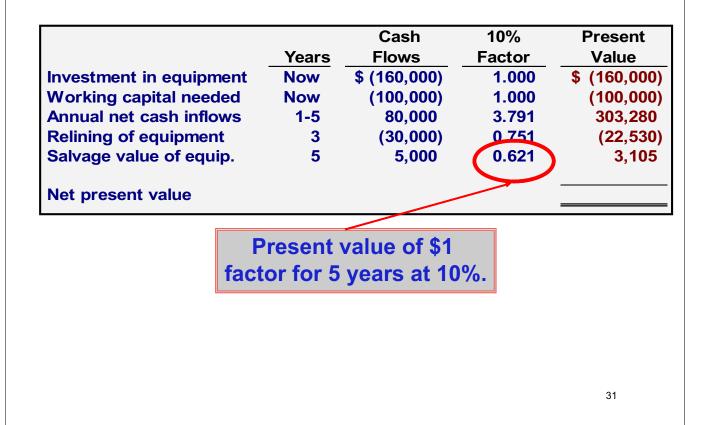
The Net Present Value Method

Investment in equipment Working capital needed	Years Now Now	Cash Flows \$ (160,000) (100,000)	10% <u>Factor</u> 1.000 1.000	Present Value \$ (160,000) (100,000)
Net present value				



The Net Present Value Method

Investment in equipr Working capital need Annual net cash inflo Relining of equipmen Net present value	ded Now ows 1-5	Cash Flows \$ (160,000) (100,000) 80,000 (30,000)	10% Factor 1.000 1.000 3.791 0.751	Present Value \$ (160,000) (100,000) 303,280 (22,530)
f	Present va actor for 3 ye			



The Net Present Value Method

		Cash	10%	Present
	Years	Flows	Factor	Value
Investment in equipment	Now	\$ (160,000)	1.000	\$ (160,000)
Working capital needed	Now	(100,000)	1.000	(100,000)
Annual net cash inflows	1-5	80,000	3.791	303,280
Relining of equipment	3	(30,000)	0.751	(22,530)
Salvage value of equip.	5	5,000	0.621	3,105
Working capital released	5	100,000	0.621	62,100
Net present value				\$ 85,955

Accept the contract because the project has a positive net present value.

Internal Rate of Return Method

- The internal rate of return is the rate of return promised by an investment project over its useful life. It is computed by finding the discount rate that will cause the net present value of a project to be zero.
- It works very well if a project's cash flows are identical every year. If the annual cash flows are not identical, a trial and error process must be used to find the internal rate of return.

General decision rule . . .

If the Interna	Rate of Return is	Then the Project is
• •	ater than the minimum rate of return	Acceptable.
	minimum required rate ⁻ return	Rejected.

When using the internal rate of return, the cost of capital acts as a hurdle rate that a project must clear for acceptance.

Internal Rate of Return Method

- Decker Company can purchase a new machine at a cost of \$104,320 that will save \$20,000 per year in cash operating costs.
- The machine has a 10-year life.

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Internal Rate of Return Method

Future cash flows are the same every year in this example, so we can calculate the internal rate of return as follows:

PV factor for the internal rate of return = Investment required Net annual cash flows

 $\frac{\$104, 320}{\$20,000} = 5.216$

Internal Rate of Return Method

Using the present value of an annuity of \$1 table . . .

Find the 10-period row, move across until you find the factor 5.216. Look at the top of the column and you find a rate of 14%.

Periods	10%	12%	14%
1	0.909	0.893	0.877
2	1.736	1.690	1.647
			1.1.1
9	5.759	5.328	4 946
(10)	6.145	5.650	→ (5.216)
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Internal Rate of Return Method

- Decker Company can purchase a new machine at a cost of \$104,320 that will save \$20,000 per year in cash operating costs.
- The machine has a 10-year life.

The internal rate of return on this project is 14%.

If the internal rate of return is equal to or greater than the company's required rate of return, the project is acceptable.

Net Present Value vs. Internal Rate of Return

NPV is easier to use.

 Questionable assumption:
 Internal rate of return method assumes cash inflows are reinvested at the internal rate of return.

Net Present Value vs. Internal Rate of Return

NPV is easier to use.

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The Total-Cost Approach

White Company has two alternatives:

(1) remodel an old car wash or,

(2) remove it and install a new one.

The company uses a discount rate of 10%.

	New Car Wash	Old Car Wash
Annual revenues	\$90,000	\$70,000
Annual cash operating costs	30,000	25,000
Net annual cash inflows	\$60,000	\$45,000

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The Total-Cost Approach

If White installs a new washer . . .

Cost	\$300,000
Productive life	10 years
Salvage value	7,000
Replace brushes at	
the end of 6 years	50,000
Salvage of old equip.	40,000

The Total-Cost Approach

Install the New Washer					
		Cash	10%		Present
	Year	Flows	Factor		Value
Initial investment	Now	\$ (300,000)	1.000	\$	(300,000)
Replace brushes	6	(50,000)	0.564		(28,200)
Net annual cash inflows	1-10	60,000	6.145		368,700
Salvage of old equipment	Now	40,000	1.000		40,000
Salvage of new equipment	10	7,000	0.386		2,702
Net present value				\$	83,202

If we install the new washer, the investment will yield a positive net present value of \$83,202.

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The Total-Cost Approach

If White remodels the existing washer . . .

Remodel costs Replace brushes at the end of 6 years

\$175,000

80,000

Let's look at the present value of this second alternative.

The Total-Cost Approach

Remodel the Old Washer						
	Cash	Cash 10%	Present			
	Year	Flows	Factor	Value		
Initial investment	Now	\$(175,000)	1.000	\$(175,000)		
Replace brushes	6	(80,000)	0.564	(45,120)		
Net annual cash inflows	1-10	45,000	6.145	276,525		
Net present value				\$ 56,405		

If we remodel the existing washer, we will produce a positive net present value of \$56,405.

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The Total-Cost Approach

Both projects yield a positive net present value.

	Present Value
Invest in new washer	\$ 83,202
Remodel existing washer	56,405
In favor of new washer	\$ 26,797

However, investing in the new washer will produce a higher net present value than remodeling the old washer.

Least Cost Decisions

In decisions where revenues are not directly involved, managers should choose the alternative that has the least total cost from a present value perspective.

Let's look at the Home Furniture Company.

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Least Cost Decisions

Home Furniture Company is trying to decide whether to overhaul an old delivery truck now or purchase a new one.

The company uses a discount rate of 10%.

Least Cost Decisions

Here is information about the trucks ...

Old Truck	
Overhaul cost now	\$ 4,500
Annual operating costs	10,000
Salvage value in 5 years	250
Salvage value now	9,000

New Truck				
Purchase price	\$ 21,000			
Annual operating costs	6,000			
Salvage value in 5 years	3,000			

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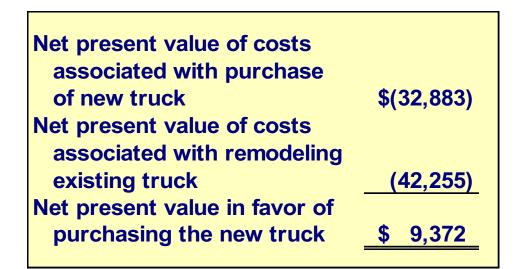
Least Cost Decisions

Buy the New Truck					
		Cash	10%	Present	
	Year	Flows	Factor	Value	
Purchase price	Now	\$ (21,000)	1.000	\$ (21,000)	
Annual operating costs	1-5	(6,000)	3.791	(22,746)	
Salvage value of old truck	Now	9,000	1.000	9,000	
Salvage value of new truck	5	3,000	0.621	1,863	
Net present value				(32,883)	

Keep the Old Truck					
	Cash	10%	Present		
Year	Flows	Factor	Value		
Now	\$ (4,500)	1.000	\$ (4,500)		
1-5	(10,000)	3.791	(37,910)		
5	250	0.621	155		
			(42,255)		
	Year Now 1-5	Cash Year Flows Now \$ (4,500) 1-5 (10,000)	Cash 10% Year Flows Factor Now \$ (4,500) 1.000 1-5 (10,000) 3.791		

Least Cost Decisions

Home Furniture should purchase the new truck.



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Other Approaches to Capital Budgeting Decisions

Other methods of making capital budgeting decisions include . . .

• The Payback Method.

Simple Rate of Return.



The payback period is the length of time that it takes for a project to recover its initial cost out of the cash receipts that it generates.

When the net annual cash inflow is the same each year, this formula can be used to compute the payback period:

Payback period = Investment required Net annual cash inflow

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The Payback Method

Management at The Daily Grind wants to install an espresso bar in its restaurant.

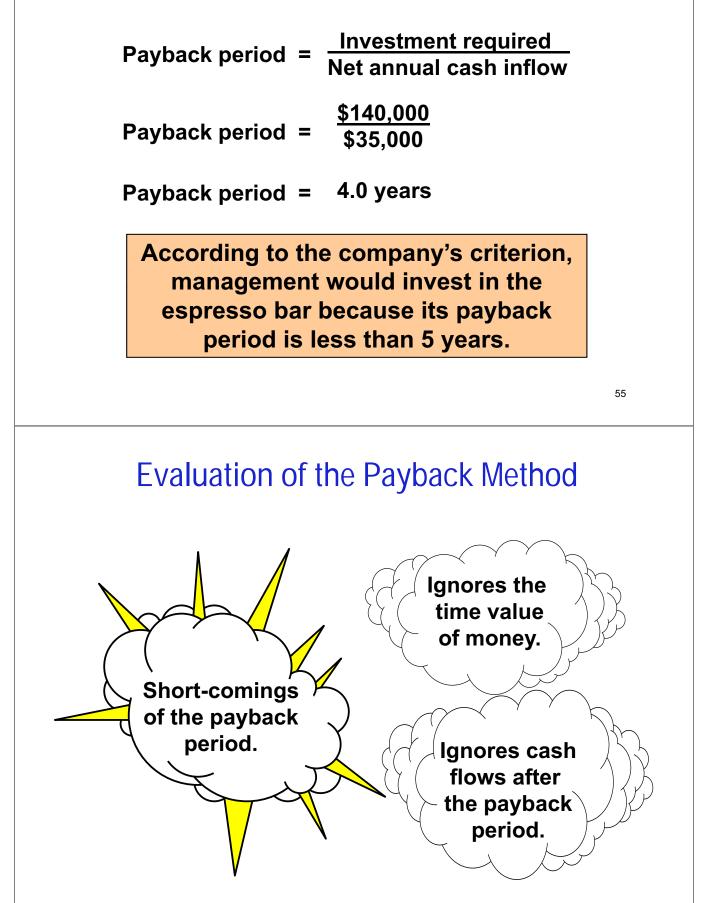
The espresso bar:

- 1. Costs \$140,000 and has a 10-year life.
- Will generate net annual cash inflows of \$35,000. 2.

Management requires a payback period of 5 years or less on all investments.

What is the payback period for the espresso bar?

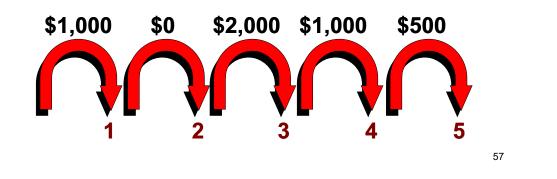
The Payback Method



Payback and Uneven Cash Flows

When the cash flows associated with an investment project change from year to year, the payback formula introduced earlier cannot be used.

Instead, the un-recovered investment must be tracked year by year.



Payback and Uneven Cash Flows

For example, if a project requires an initial investment of \$4,000 and provides uneven net cash inflows in years 1-5 as shown, the investment would be fully recovered in Yr. 4.

