

# MATH 234A : COMPLEX ANALYSIS

California State University, Sacramento · Department of Mathematics & Statistics

Complex numbers, complex functions, analytic functions, complex integration, harmonic functions.

## CATALOG DESCRIPTION

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Complex numbers, complex functions, analytic functions, complex integration, harmonic functions. **Graded:** Graded Student. **Units:** 3.0.

## PREREQUISITES

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Math 130B; Math 134 or 105B recommended.

## COURSE OUTLINE

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### I. Complex Numbers

- A. Complex number system
- B. Complex plane
- C. Extended complex plane

### II. Elementary Functions

- A. Powers
- B. Roots
- C. Exponential and logarithmic functions

### III. Elementary Point Set Topology

### IV. Analytic Functions

- A. Limits, continuity, differentiation
- B. Elementary theory of power series
- C. Uniform convergence
- D. Conformity
- E. Linear fractional transformation

### V. Complex Integration

- A. Complex integral
- B. Cauchy's theorem for triangle, rectangle, disk
- C. Cauchy's integral formula
- D. Local properties of analytic functions
- E. General form of Cauchy's Theorem
  - 1. Index of a point with respect to a closed curve
  - 2. Chains and cycles

3. Homology

F. Calculus of residues

VI. Harmonic Functions

A. Mean-value property

B. Poisson's formula

C. Schwarz's theorem

D. Reflection principle

Sample